

# Dynamics of Secured and Unsecured Debt Over the Business Cycle

Paul Luk, Hong Kong Baptist University  
Tianxiao Zheng, SAIF, Shanghai Jiao Tong University

## Introduction

- Firms have heterogeneous debt structure.
- Unsecured debt is much more procyclical than secured debt. (Azariadis, Kaas and Wen, 2016)
- We depart from standard macro-finance setups by modelling heterogeneous debt structure in firms.

## Main Findings

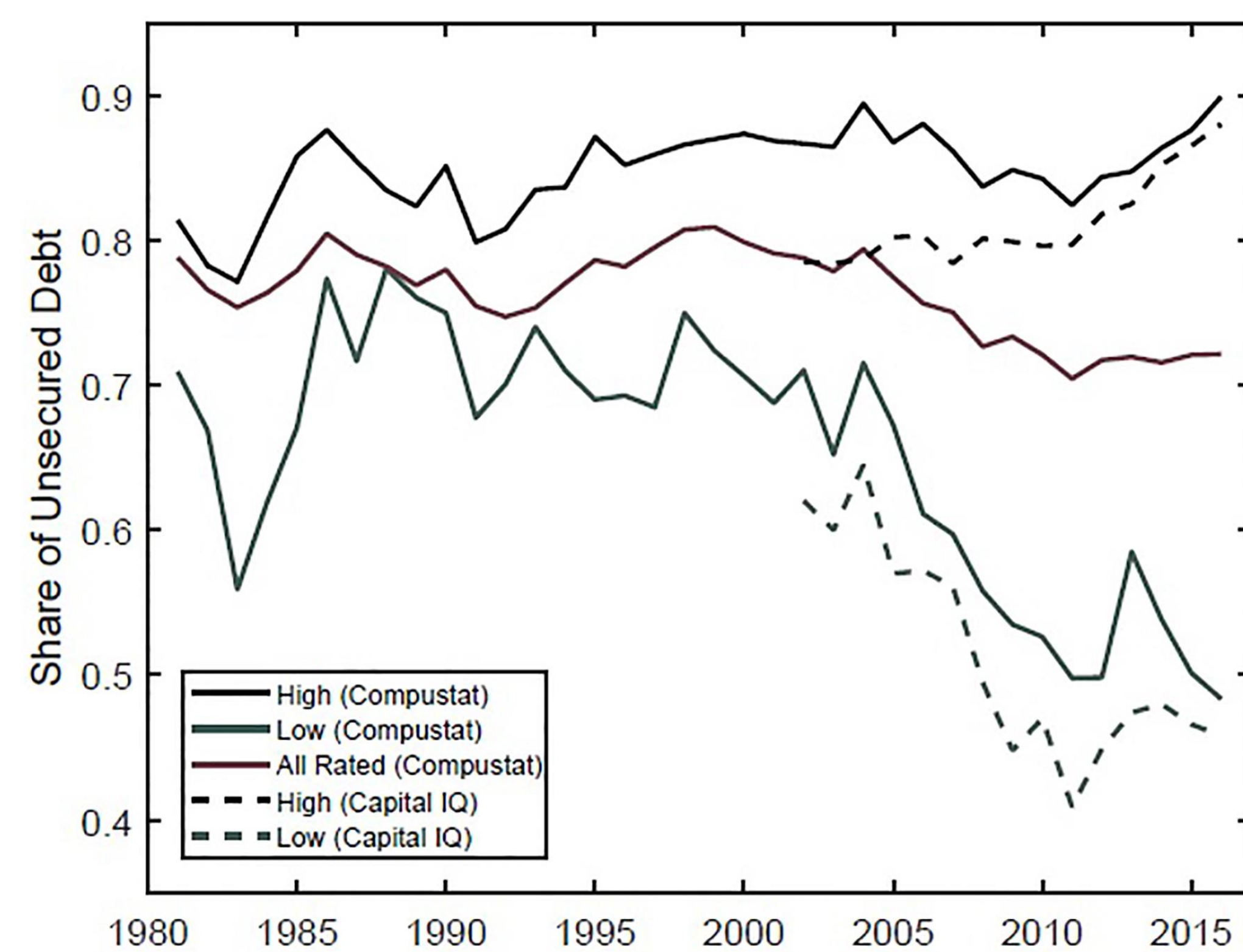
- Borrowers and lenders in unsecured debt contracts are more cautious relative to secured debt.
- The model matches following stylized facts:
  - High-credit-quality firms have lower leverage.**
  - Unsecured debt is procyclical.**
  - Secured debt is acyclical.**
- Financial accelerator mechanism associated with unsecured debt has less amplification than Bernanke et al. (1999).

## Stylized facts

- Public traded non-financial and non-utility US firms with long-term credit rating. (Source: Compustat)
- 1142 rated firms in 1981-2017 (annual).  
Secured debt = 'mortgage and other secured debt'  
Unsecured debt = 'long-term debt + total current debt' – Secured debt

## Leverage Ratios Across Quality Distribution

	Leverage			Leverage	
AA and above	1.53	B- and below	1.95		
BBB and above	1.62	CCC and below	2.13		
BBB- and above	1.65	CC and below	2.31		



Corr (Y, Debt)	Rated Firms	All Obs.	Model
Secured Debt	0.06	0.15	0.09
Unsecured Debt	0.48	0.50	0.64

## Model: Credit Contracts

- We embed heterogeneous firms and secured & unsecured debt in a RBC model.
- Firm  $j \in [0, 1]$  has return on capital  $\omega_{jt}R_t^K$ .
- $\log(\omega_{jt}) \sim N(-0.5\sigma_{t-1}^2, \sigma_{t-1}^2)$ , with  $E(\omega_{jt}) = 1$ .
- Each firm carries a publicly observed label  $i \in [G, B]$ .
- A G firm can borrow both secured and unsecured debt. (In eqm., G firms only borrow unsecured debt.)
- A B firm can only borrow secured debt.

## Secured Debt

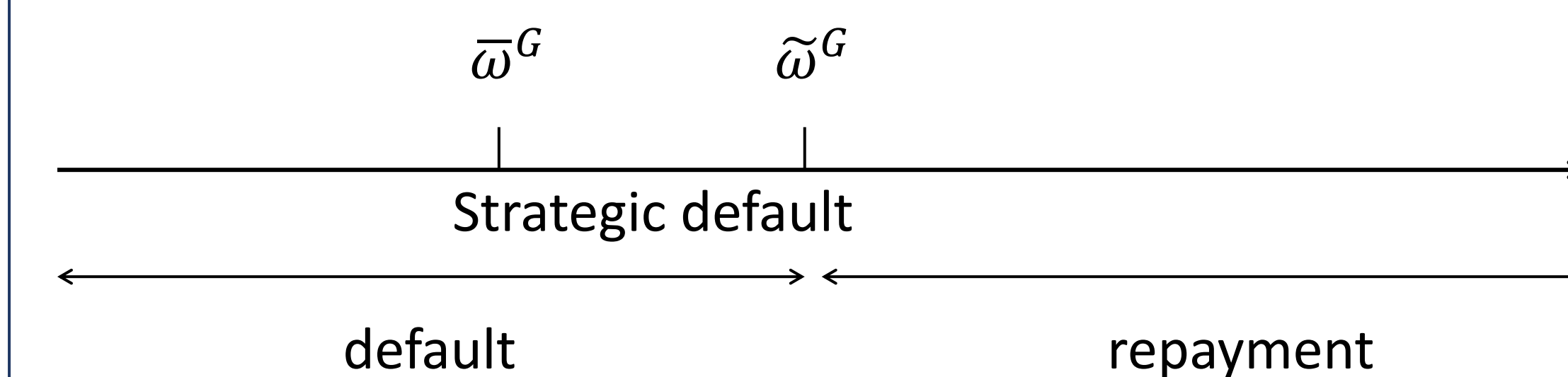
- Define  $\bar{\omega}_{jt}^B$ . A B firm can repay if  $\omega_{jt} \geq \bar{\omega}_{jt}^B$ .

	$\omega_{jt} \leq \bar{\omega}_{jt}^B$	$\omega_{jt} > \bar{\omega}_{jt}^B$
B firm	Default and bankrupt.	Repay loan. Keep profit.
Lender	Get liquidation value of the firm.	Receive repayment.

## Unsecured Debt

- Define  $\bar{\omega}_{jt}^G$ . A G firm can repay if  $\omega_{jt} \geq \bar{\omega}_{jt}^G$ .
- A G firm chooses to repay when  $\omega_{jt} \geq \bar{\omega}_{jt}^G$ .

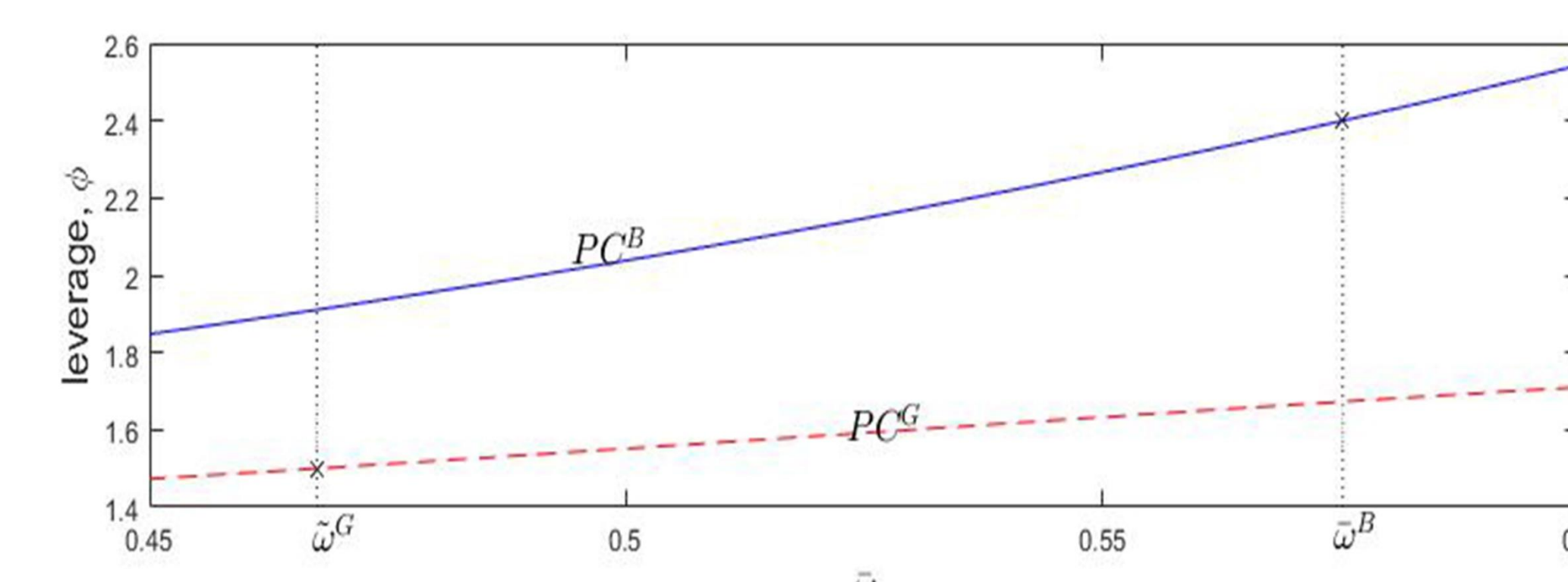
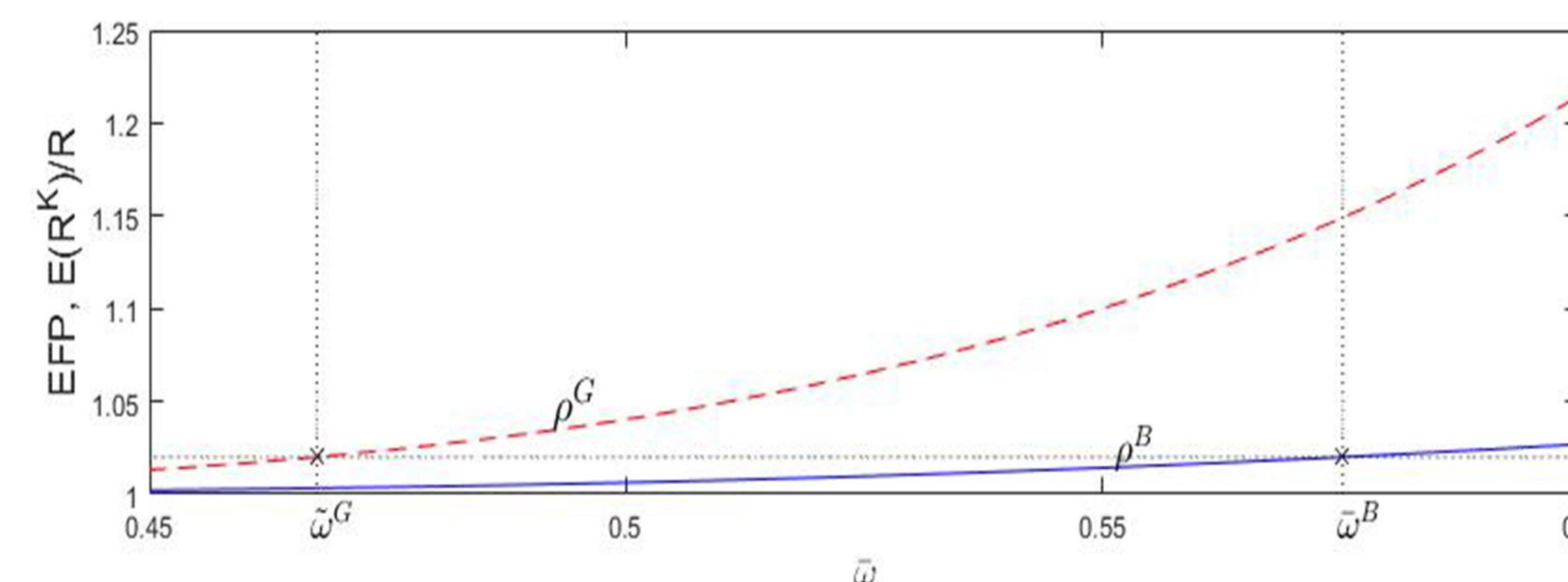
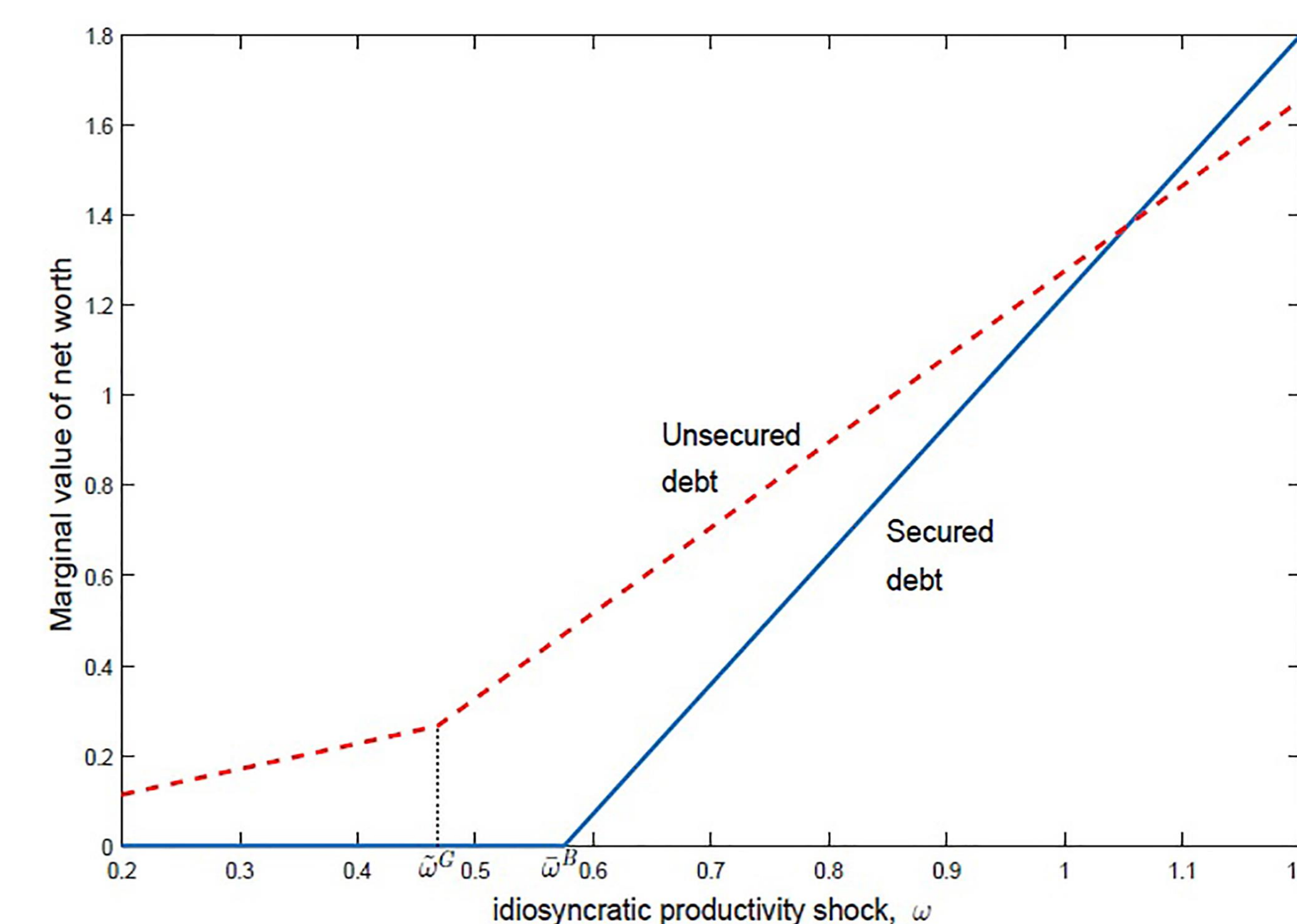
	$\omega_{jt} \leq \bar{\omega}_{jt}^G$	$\omega_{jt} > \bar{\omega}_{jt}^G$
G firm	Default: With $Pr = \zeta$ , keep assets and becomes B firm; With $Pr = (1 - \zeta)$ , gets nothing.	Repay loan. Keep profit.
Lender	Gets zero return.	Receive repayment.



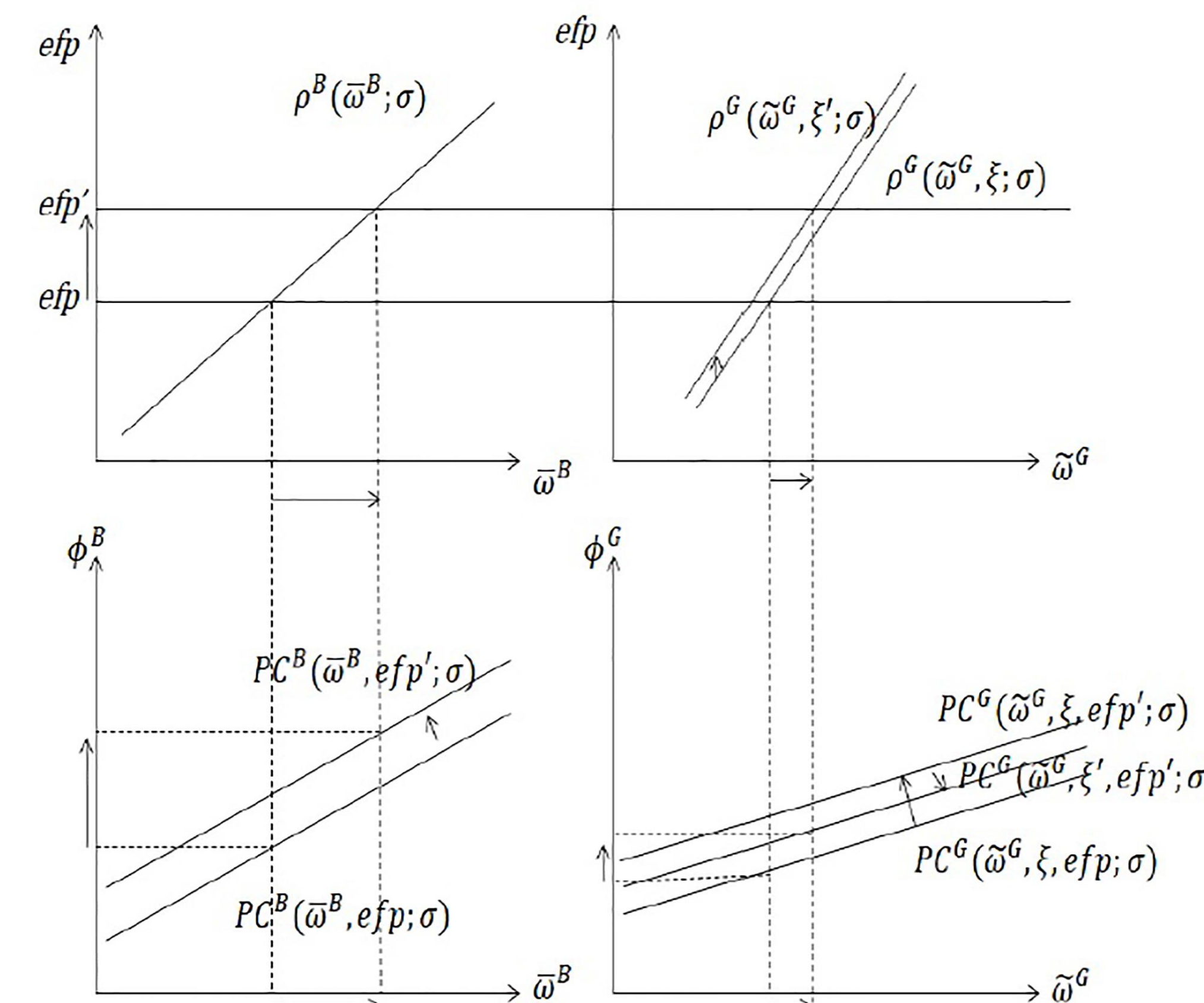
## The Optimal Contract

- Each firm maximizes its continuation value subject to lenders' participation constraint (PC).
- Value of a firm is given by  $V_t^i(N_{jt}^i) = \lambda_t^i N_{jt}^i$ , for  $i \in \{G, B\}$ , where  $\lambda_t^G > \lambda_t^B > 1$ .
- All  $i \in \{G, B\}$  firms choose same leverage,  $\phi_t^i$ .
- All G firms choose same default strategy:  $\xi_t \bar{\omega}_t^G = \bar{\omega}_t^G$ , where  $\xi_t < 1$  and  $\xi_t'(\lambda_t^G/\lambda_t^B) > 0$ .

- Secured debt borrowers worry less about downside risks, so B firms' FOC  $\rho^B$  is less steep than G firms'.
- Secured debt lenders worry less about downside risks too, so B firms' PC is steeper than G firm's PC.
- So, for a given  $R^K$ , B firms have higher leverage.



- Given relative slopes, a bad shock increases  $\phi^B$  more.
- Debt is increasing in net worth and leverage ( $B_t = (\phi_t - 1)N_t$ ), so secured debt is less procyclical.



## Calibration

Annual frequency.

Financial market SS targets:

(a)  $R^K/R=2\%$ , (b)  $B^G/B=0.75$ , (c)  $\phi^B=2.4$ , (d)  $\phi^G=1.5$ .

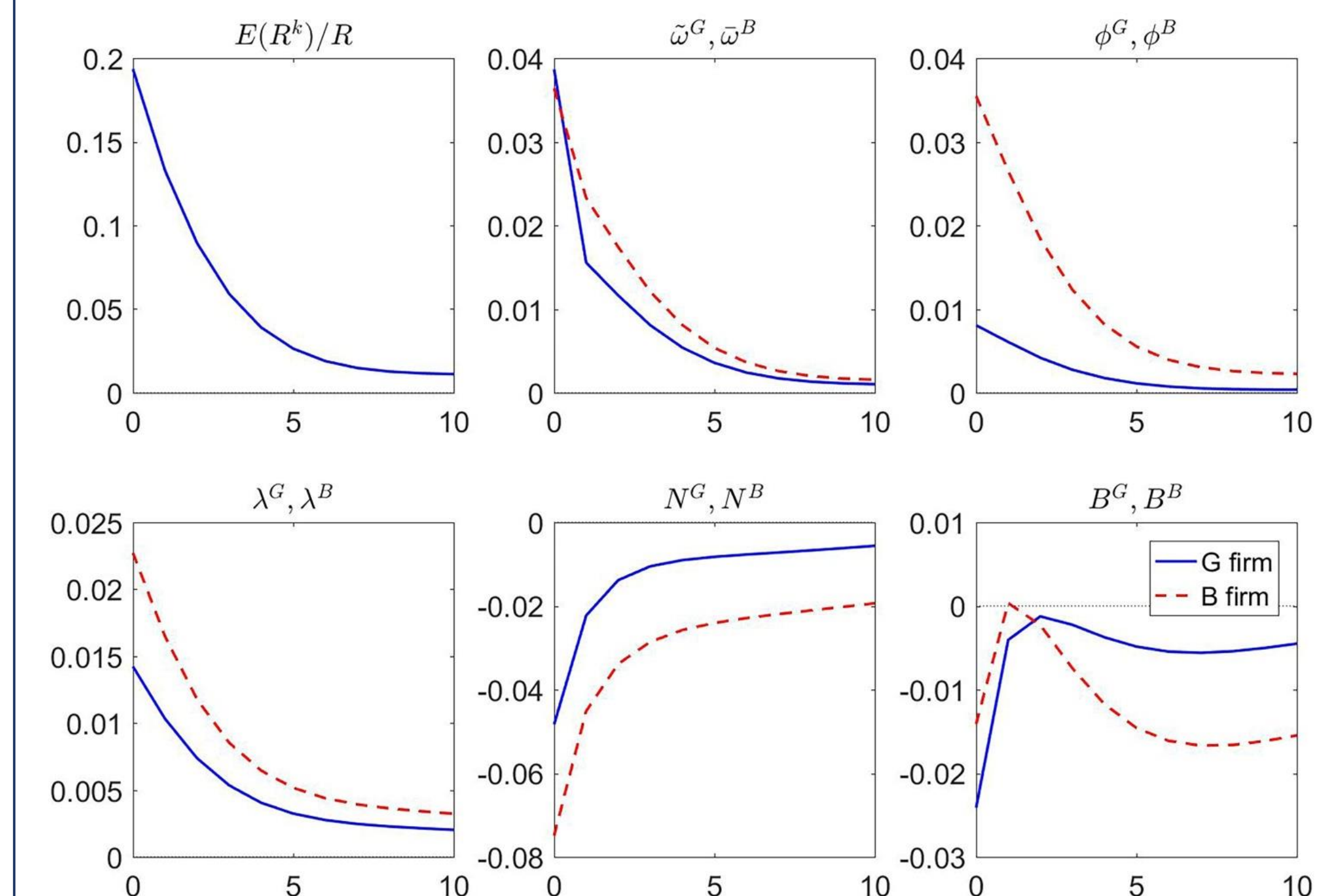
Parameter	Value	Meaning
$\theta$	0.87	Firm survival probability
$\kappa$	0.017	Initial monitoring cost for secured debt
$\mu$	0.2	Liquidation costs
$\zeta$	0.388	Debt restructuring success rate
$\bar{\sigma}$	0.257	Std. dev of idiosyncratic shock
$\Upsilon$	0.068	Firm initial transfer

TFP shocks ( $A_t$ ):  $\rho_A = 0.56, s_A = 0.023$ .

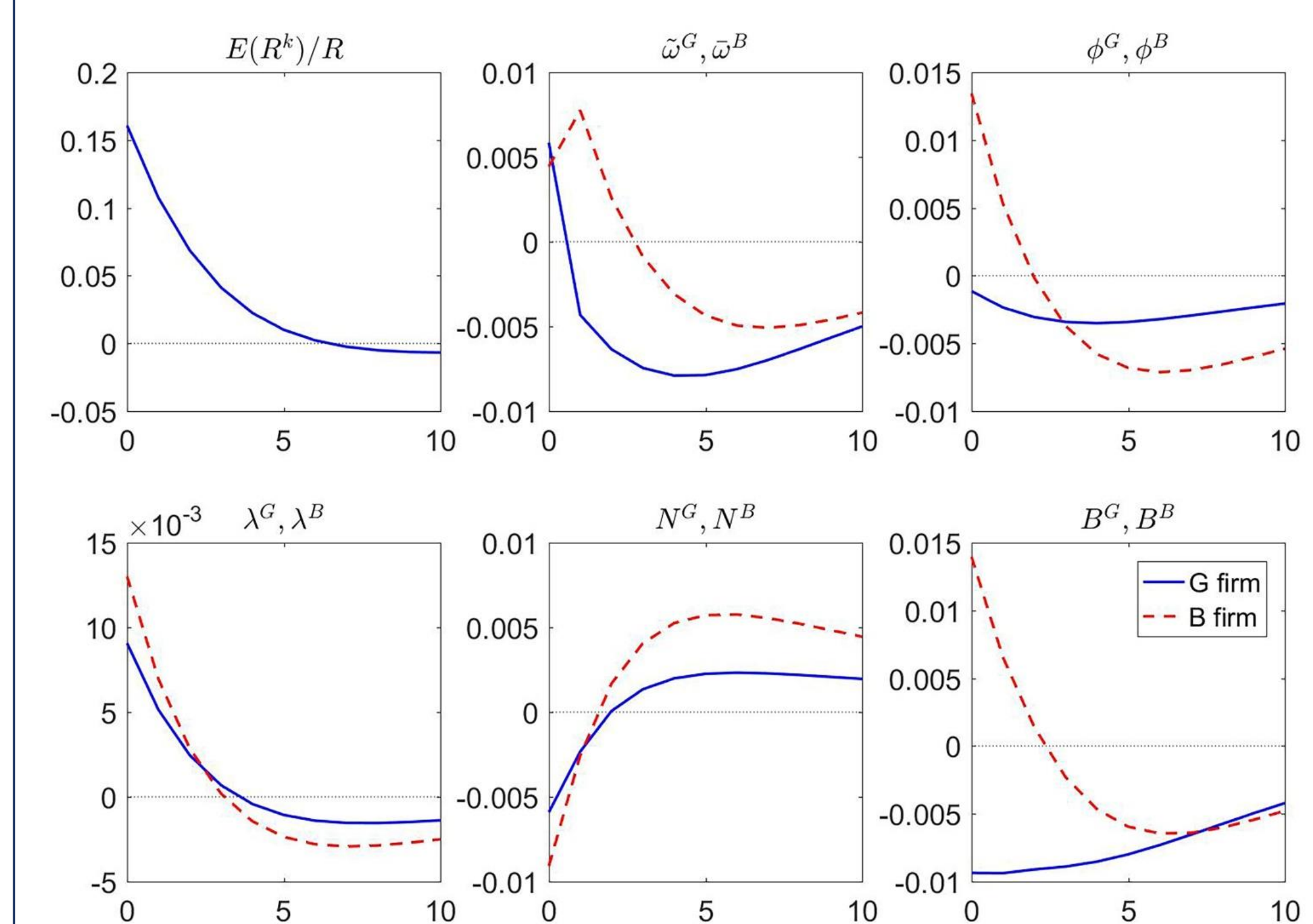
Volatility shocks ( $\sigma_t$ ):  $\rho_\sigma = 0.85, s_\sigma = 0.026$ .

## Results

### TFP Shock



### Volatility Shock



## Conclusions

- We document stylized facts about corporate firms' debt structure.
- We build a model with heterogeneous debt structure, and it matches key stylized facts.
- Dynamics of unsecured debt are important in understanding business cycles.